

# THERMAL MATTER

## Thermal Expansion

Linear Expansion	Areal Expansion	Volume Expansion
$\alpha = \frac{\Delta l}{l\Delta T}$	$\beta = \frac{\Delta A}{A\Delta T}$	$\gamma = \frac{\Delta V}{V\Delta T}$
$\alpha$ = coefficient of linear expansion $\Delta l$ = change in length $\Delta T$ = rise in temp	$\beta$ = coefficient of areal expansion $\Delta A$ = change in length	$\gamma$ = coefficient of volume expansion $\Delta V$ = change in volume

Relation between  $\alpha$ ,  $\beta$  and  $\gamma$

$$\alpha = \frac{\beta}{2} = \frac{\gamma}{3}$$

Measurement of Temperature

$$\frac{C}{100} = \frac{F - 32}{180} = \frac{K - 273}{80}$$

## Construction of Thermometer

If length of mercury column at  $0^\circ$  and  $100^\circ$  are  $l_0$  and  $l_{100}$  respectively and at  $t^\circ$  the length of mercury is  $l_t$

$$\frac{l_t - l_0}{t} = \frac{l_{100} - l_0}{100}$$



## Specific Heat Capacity (S)

Heat capacity per gram of substance	$Q = mS\Delta T$ $m$ =mass of substance $Q$ =Heat Required $\Delta T$ =Change in temperature
Specific Heat capacity of water	4.184 J/g <sup>o</sup> or 1 cal/g <sup>o</sup>
Molar Specific Heat Capacity	$c = \frac{\Delta Q}{\mu\Delta T}$ $\mu$ =No. of moles of substance

## Latent Heat

$m$ =mass of substance $L$ =Latent Heat of Substance $Q$ =Heat required	$Q = mL$
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## Principle of Calorimetry

When a hot body is mixed with cold body, then heat lost by hot body is equal to the heat gained by cold body

$$T_{\text{mix}} = \frac{m_1 c_1 T_1 + m_2 c_2 T_2}{m_1 c_1 + m_2 c_2}$$

## Transmission of Heat

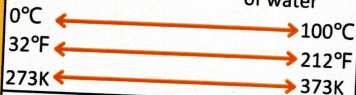
<b>Thermal Conductivity</b> $K$ =coefficient of thermal conductivity $A$ =area of cross-section $l$ =length of rod, $t$ =time $\Delta\theta$ =temperature difference b/w the end of the rod	$Q = \frac{KA\Delta\theta t}{l}$
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## Ideal Gas Equation

$$PV = nRT$$

Freezing point  
of water

Boiling point  
of water



**Measurement of Temperature**

$$\frac{T - T_{FP}}{T_{BP} - T_{FP}}$$

$$\frac{\text{Reading on scale} - \text{Lower fixed point}}{\text{Higher fixed point} - \text{Lower fixed point}} = \text{constant}$$

## Specific Heat Capacity

$$S_{\text{water}} = 1 \text{ cal/gC}^\circ$$

$$S_{\text{ice}} = \frac{1}{2} \text{ cal/gC}^\circ$$

$$S_{\text{steam}} = \frac{1}{2} \text{ cal/gC}^\circ$$

$$1 \text{ cal} = 4.2 \text{ J}$$

High specific heat capacity  $\rightarrow$  Good Coolant

**Latent Heat**

$$L_{\text{fusion}} = \text{solid} \leftrightarrow \text{liquid} = 80 \text{ cal/g}$$

$$L_{\text{vap}} = \text{liquid} \leftrightarrow \text{gas} = 540 \text{ cal/g}$$

**Thermal Stress**

$$\sigma = Y\alpha\Delta T$$

( $\sigma=0$ , for freely expanding rod)

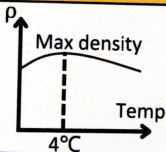
## Reading of scale

$$\text{True length} = \text{Reading} [1 + (\alpha_s - \alpha_r)\Delta T]$$

$\alpha_s$  = Thermal coefficient of linear expansion of scale

$\alpha_r$  = Thermal coefficient of linear expansion of rod

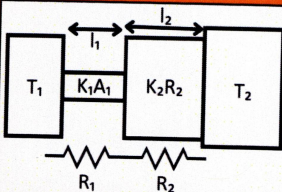
**Anomalous behaviour of water**



**Thermal gradient**

$$\Delta T/l$$

**Current in series**



Here,  $R_{eq} = R_1 + R_2$

$$= \frac{l_1}{K_1 A_1} + \frac{l_2}{K_1 A_1}$$

Then,

$$I = \frac{T_1 - T_2}{R_{eq}}$$

**Rate of heat loss**

where,  
e=emissivity

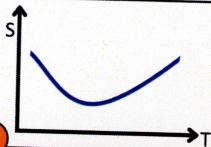
$$\sigma e A (T^4 - T_0^4)$$

$$0 < e \leq 1$$

**Emissive Power**

$$E = \frac{\text{Energy}}{\text{Area} \times \text{Time}}$$

**Variation of specific heat capacity of water with temperature**





## Variation of time period of pendulum clocks

Gain/Loss in time  
duration 't'

$$\Delta t = \frac{1}{2} \alpha \Delta \theta \cdot t$$

$$\Delta \theta = \theta - \theta_0$$

$\theta_0$  = original temperature at time period T

$\theta$  = increased temperature at time period T

Cases

$$\theta < \theta_0$$

$$T' > T$$

- Clock becomes fast & gain time

$$\theta > \theta_0$$

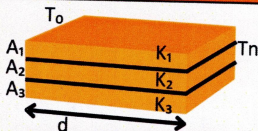
$$T' < T$$

- Clock becomes slow & loose time

Specific Heat & water equivalent

$$W = mS$$

Current in parallel



$$I = \frac{(T_0 - T_n)(K_1 A_1 + K_2 A_2 + K_3 A_3)}{d}$$

Absorptive power

$$a = \frac{\text{Energy absorbed}}{\text{Energy incident}}$$

Spectral Emission Power

$$E = \int_0^{\infty} E_{\lambda} d\lambda$$